# Unified Growth Theory and Comparative Development

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Economic Growth and Comparative Development

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- What is the role of deep-rooted factors in explaining the observed patterns of comparative development?

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  - Importance of deep-rooted factors in comparative development

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  - Existing hypotheses about the role of geographical, cultural, institutional and genetic factors in comparative development

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  - Vanishing Malthusian equilibrium

• Evolution of a latent state variable - the demand for human capital

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    - The economy gravitates towards the emerging Modern Growth Regime

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    - the rate of technological progress

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  - Determined by households' decisions about the number and level of human capital of their children

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- Output per capita fluctuates (with a negligible trend) around a constant level in the long-run
  - Reflecting diminishing returns to labor & positive effect of income on population

#### Production

• The output produced in period *t* 

$$Y_t = H_t^{\alpha} (A_t X)^{1-\alpha}$$

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- $X \equiv land$
- Output per worker produced at time t

$$y_t = h_t^{\alpha} x_t^{1-\alpha}$$

- $h_t \equiv H_t/L_t \equiv$  efficiency units per-worker
- $x_t \equiv (A_t X)/L_t \equiv$  effective resources per worker

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- Long-run (population reaches a new steady-state):
  - $L_t \uparrow \Longrightarrow y \downarrow \text{ (back to } \bar{y}\text{)}$

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Later Stages of Development

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 Educated individuals have an advantage in adopting and advancing new technologies

$$g_{t+1} \equiv \frac{A_{t+1} - A_t}{A_t} = g(e_t, L_t)$$

- $g_{t+1} \equiv$  rate of tech progress
- $\bullet$   $e_t \equiv$  education
- $L_t \equiv$  population size

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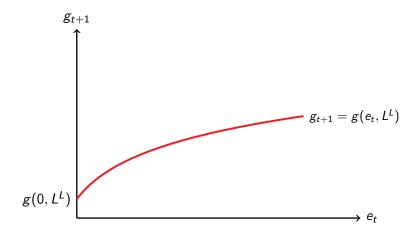
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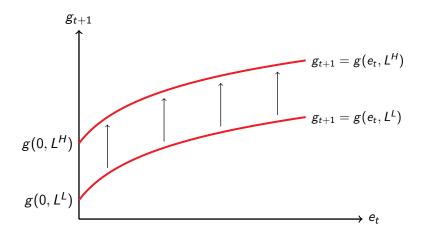
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  - The scale of the economy has a positive and diminishing effect on technological progress
- g(0, L) > 0 for L > 0
  - Technological progress is positive at the outset





### The Effect of Population Size on Technological Progress



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  - Human capital permits individuals to better cope with the changes in the technological environment
  - The introduction of new technologies is skill-biased in the short-run, although the nature of the technology can be skill-biased or skill-saving in the long run

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- $g_{t+1} \equiv$  rate of tech progress

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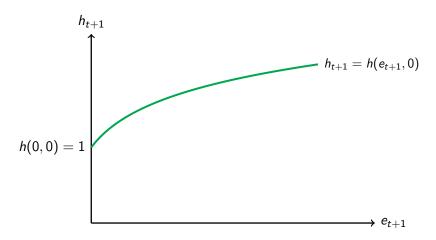
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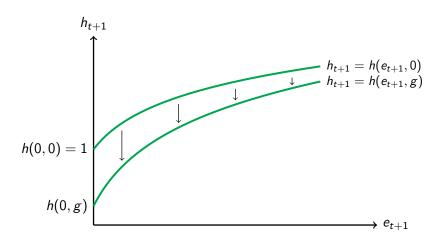
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  - Education lessens the obsolescence of HC in a changing technological environment
- h(0,g) > 0
  - Basic level of human capital





## Effect of Technological Progress on Human Capital Formation



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    - Population growth declines & human capital formation increases further

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#### **Preferences**

The utility function of individual t (adult at time t)

$$u^t = (1 - \gamma) \ln(c_t) + \gamma \ln(n_t h_{t+1})$$

- $c_t \equiv$  consumption of individual t
- $n_t \equiv$  number of children of individual t
- $h_{t+1} \equiv$  level of human capital of each child

## **Budget and Subsistence Consumption Constraints**

$$z_t n_t (\tau + e_{t+1}) + c_t \le z_t$$

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## **Budget and Subsistence Consumption Constraints**

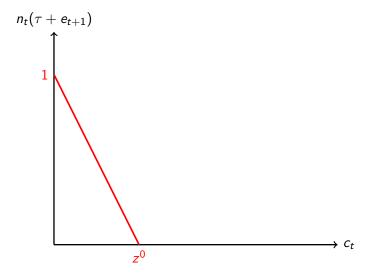
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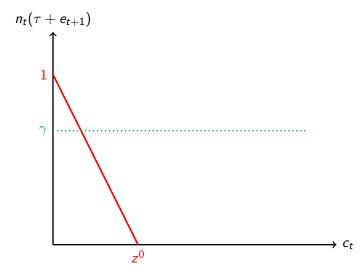
- $z_t \equiv$  potential income of individual t
- $\bullet$   $\tau \equiv$  time required to raise a child, regardless of quality
- $\tau + e_{t+1} \equiv$  time needed to raise a child with education  $e_{t+1}$

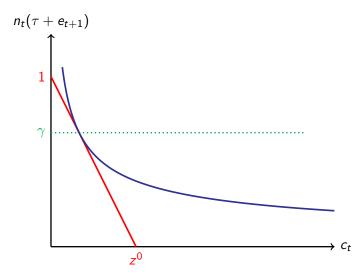
$$z_t \equiv y_t = h_t^{\alpha} x_t^{1-\alpha} = z(e_t, g_t, x_t)$$

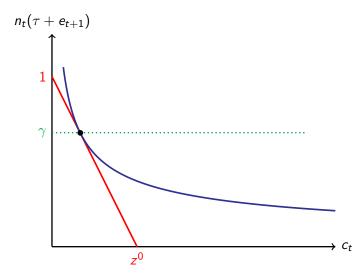
• Subsistence consumption constraint:

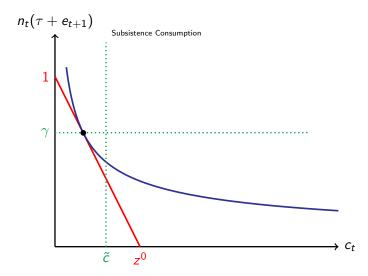
$$c_t \geq \tilde{c}$$

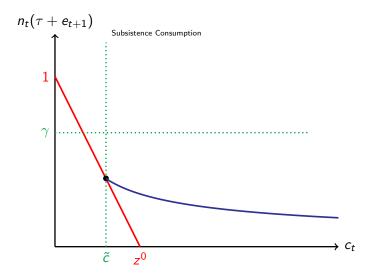


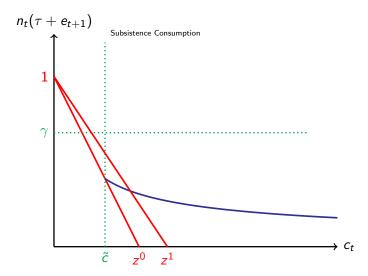


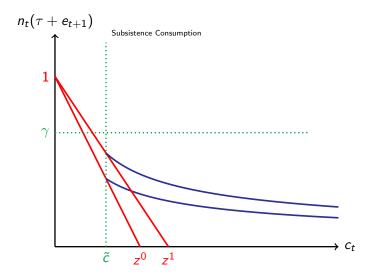


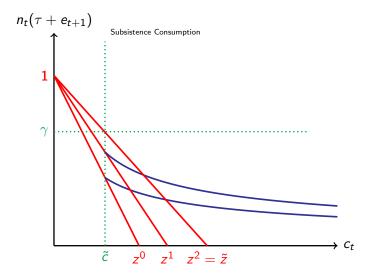


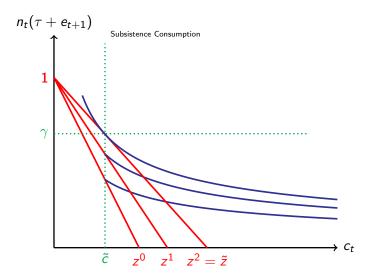


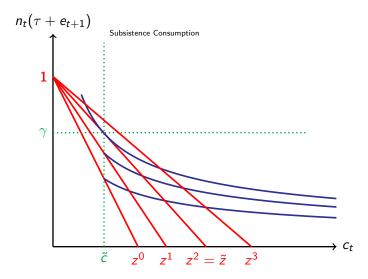


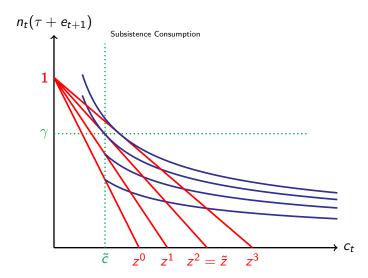


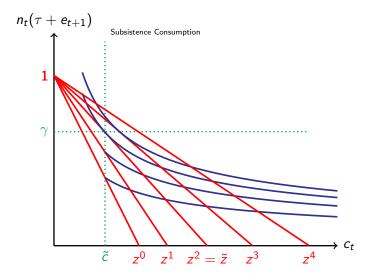


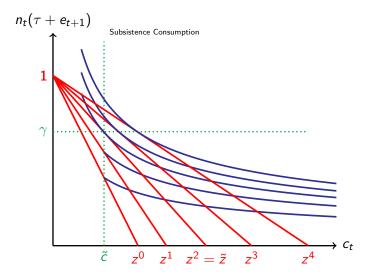


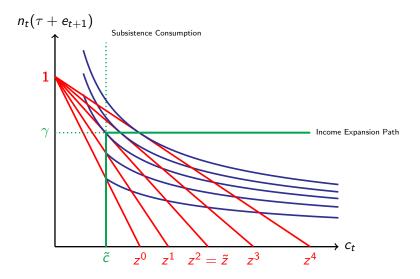








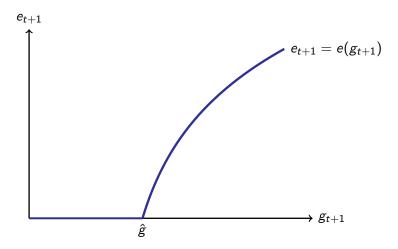




# Optimal Investment in Child Quality



# Optimal Investment in Child Quality



#### Optimization: Quantity and Quality of Children

• Time devoted to children:

$$n_t( au+e_{t+1}) = \left\{egin{array}{ll} \gamma & ext{if} & z_t \geq ilde{z} \ & & \ 1-rac{ ilde{c}}{z_t} & ext{if} & z_t \leq ilde{z} \end{array}
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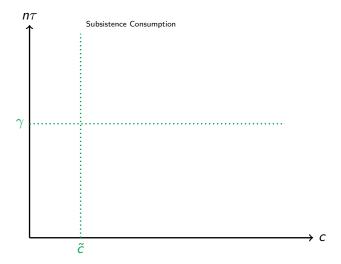
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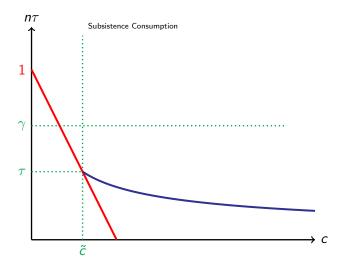
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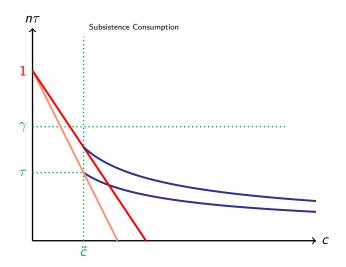
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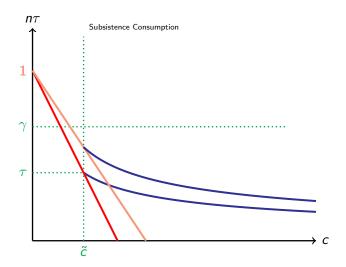
$$e_{t+1} = e(g_{t+1}) \Longrightarrow$$
 
$$n_t = \begin{cases} \frac{\gamma}{\tau + e(g_{t+1})} \equiv n^b(g_{t+1}) & \text{if} \quad z_t \geq \tilde{z} \\ \\ \frac{1 - [\tilde{c}/z_t]}{\tau + e(g_{t+1})} \equiv n^a(g_{t+1}, z(e_t, g_t, x_t)) & \text{if} \quad z_t \leq \tilde{z} \end{cases}$$

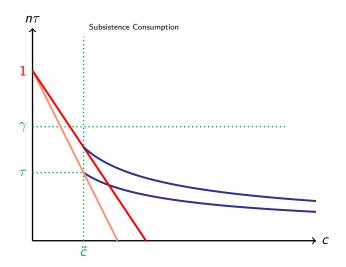


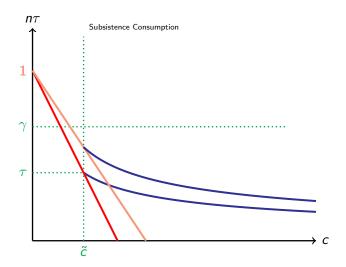


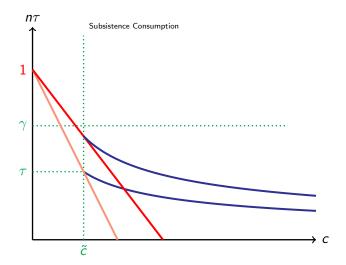


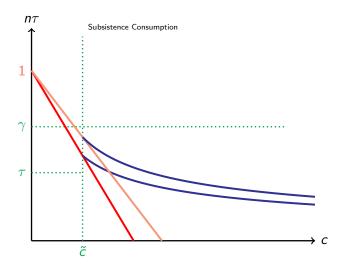


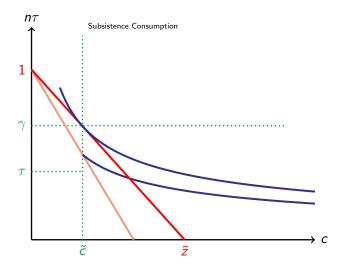




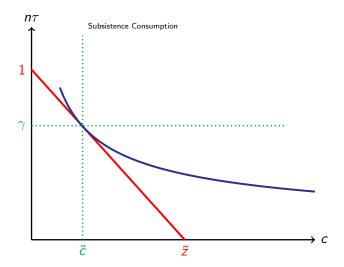




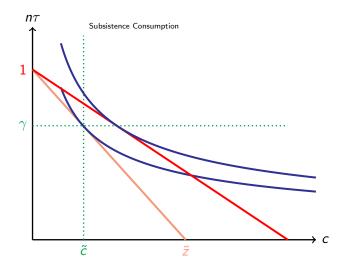




### Post-Demographic Transition



## Post-Demographic Transition



#### Population Dynamics

$$L_{t+1} = n_t L_t$$

$$L_{t+1} = \left\{ egin{array}{ll} n^b(g_{t+1})L_t & ext{if} \quad z_t \geq ilde{z} \ \\ n^a(g_{t+1}, z(e_t, g_t, x_t))L_t & ext{if} \quad z_t \leq ilde{z} \end{array} 
ight.$$

#### Dynamics of the Level of Resources per Worker

$$x_{t+1} = \frac{A_{t+1}X}{L_{t+1}} = \frac{(1+g_{t+1})A_tX}{n_tL_t} = \frac{1+g_{t+1}}{n_t}x_t$$

$$x_{t+1} = \begin{cases} \frac{[1+g(e_t,L_t)][\tau^q + \tau^e e(g(e_t,L_t))]}{\gamma} x_t \equiv \phi^b(e_t;L_t) x_t & z_t \geq \tilde{z} \\ \frac{[1+g(e_t,L_t)][\tau + e(g(e_t,L_t))]}{1-[\tilde{c}/z(e_t,g_t,x_t)]} x_t \equiv \phi^a(e_t,g_t,x_t,L_t) x_t & z_t \leq \tilde{z}, \end{cases}$$

#### The Dynamical System

A sequence  $\{x_t, e_t, g_t, L_t\}_{t=0}^{\infty}$  such that:

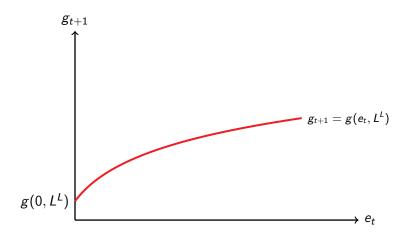
$$\begin{cases} x_{t+1} = \phi(e_t, g_t, x_t, L_t) x_t \\ e_{t+1} = e(g(e_t, L_t)) \\ g_{t+1} = g(e_t, L_t) \\ L_{t+1} = n(e_t, g_t, x_t, L_t) L_t \end{cases}$$

#### The Conditional Evolution of Technology and Education

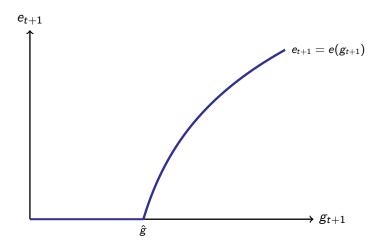
A sequence  $\{g_t, e_t; L\}_{t=0}^{\infty}$  such that:

$$\left\{egin{array}{l} g_{t+1}=g(e_t;L) \ & \ e_{t+1}=e(g_{t+1}) \end{array}
ight.$$

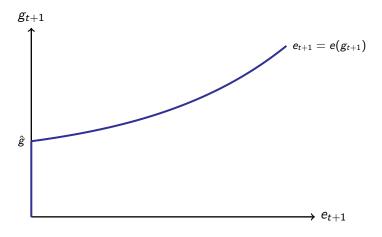
# The Effect of Education on Technology



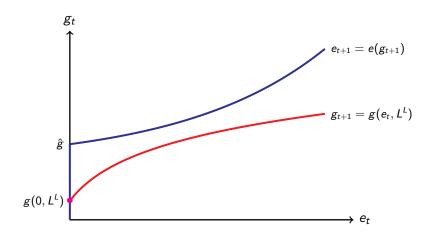
### The Effect of Technology on Education



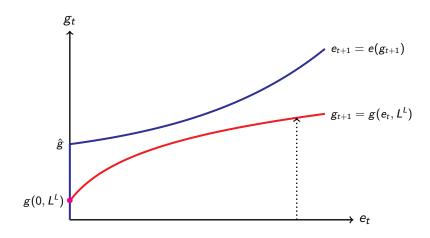
### The Effect of Technology on Education: Flipped Axis



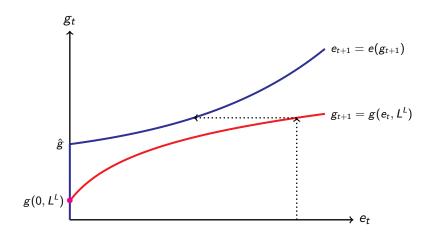
#### The Evolution of Education and Technology: For a Given Population Size

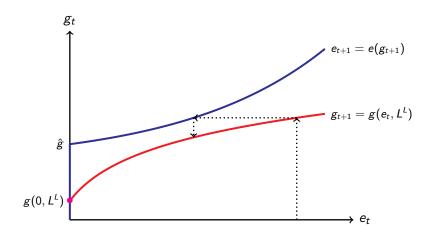


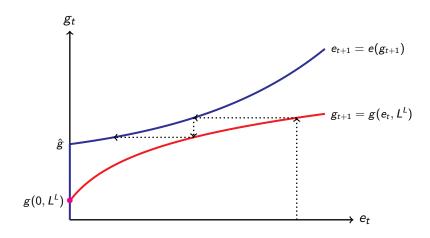
#### The Evolution of Education and Technology: For a Given Population Size

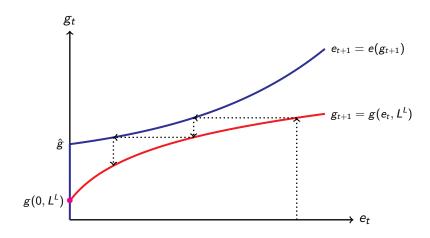


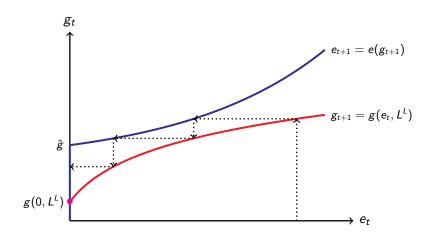
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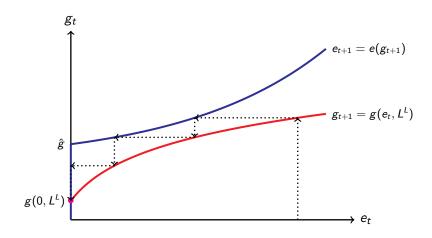


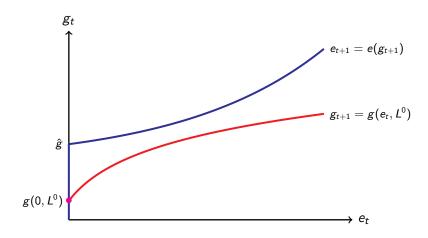


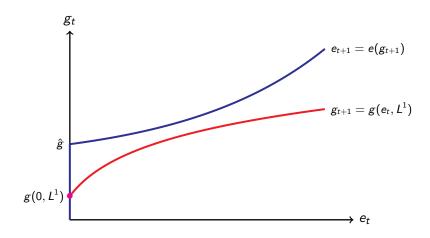


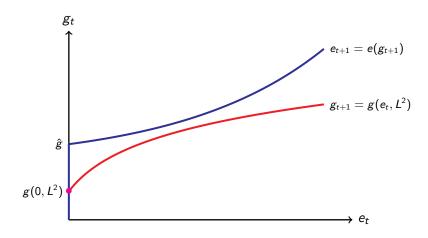


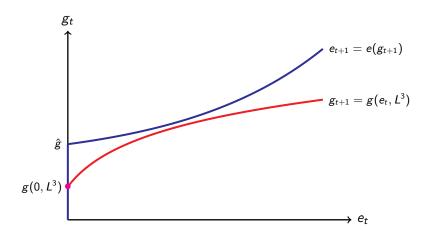


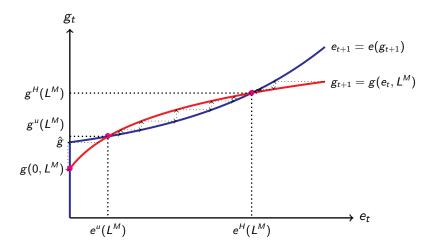


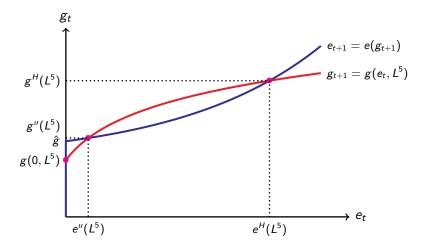


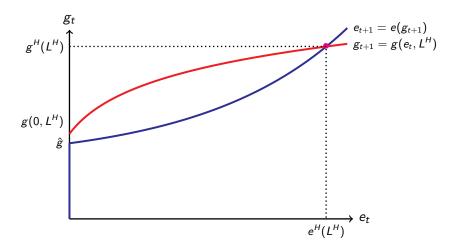


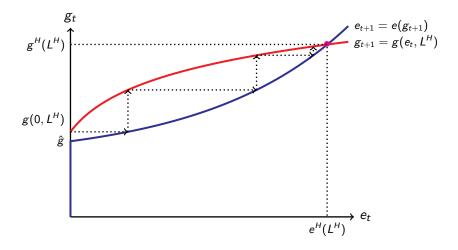




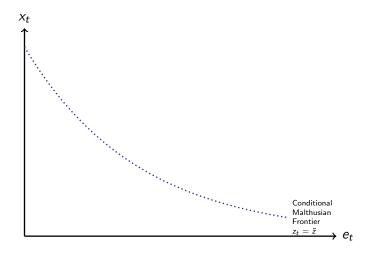


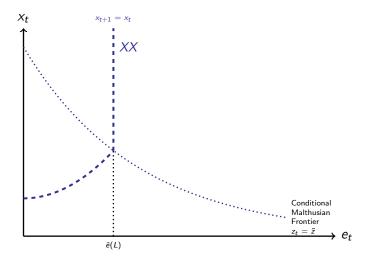


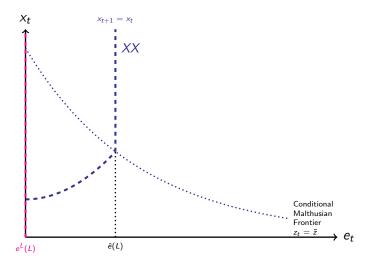


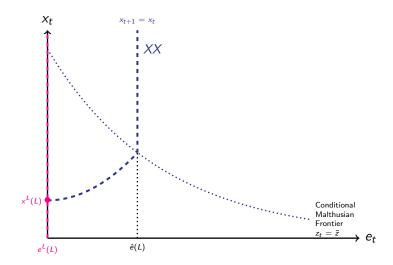


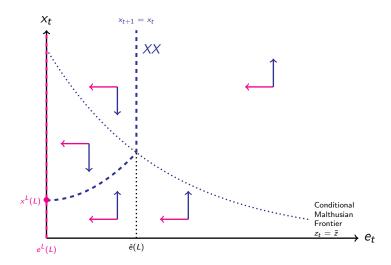


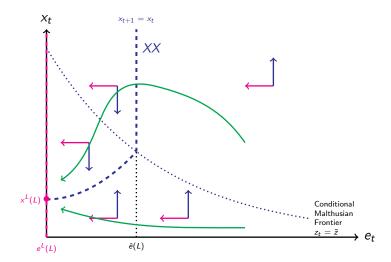


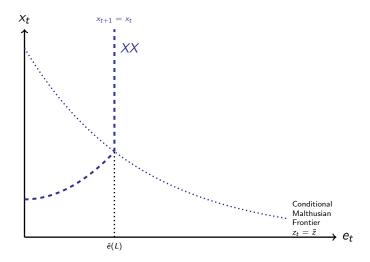


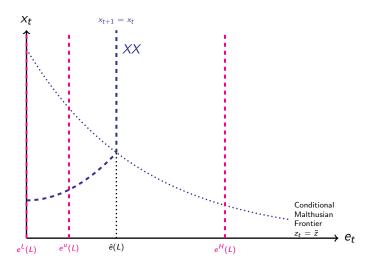


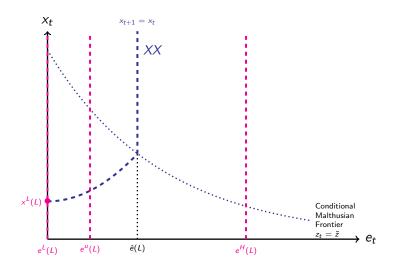


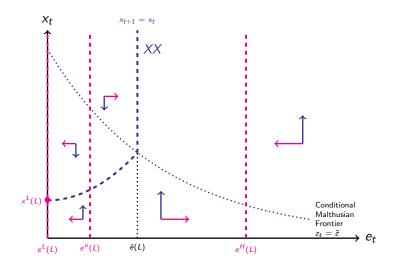


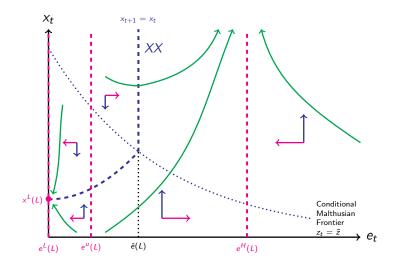


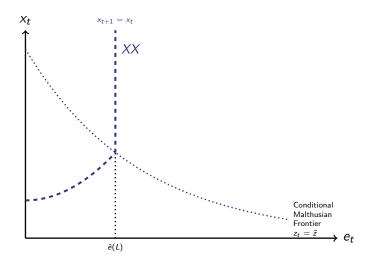


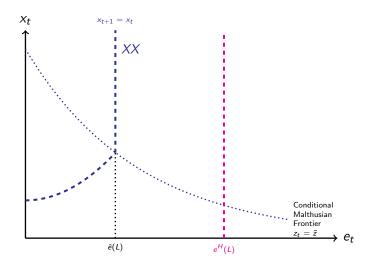


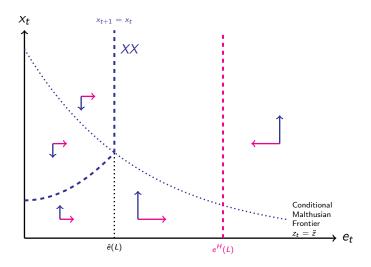


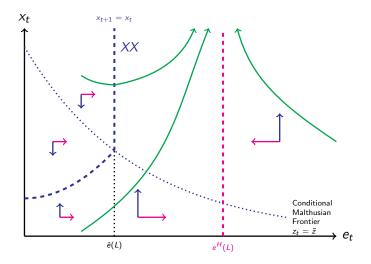




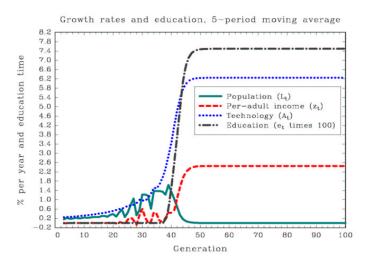








#### Simulation



Source: Lagerlöf (RED 2006)

• The Malthusian interaction between technology & population

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  - Acceleration in technological progress

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    - ⇒ Economic growth is freed from counterbalancing effects of population
  - Technological progress, human capital & decline in population growth
    - ⇒ Sustained economic growth

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    - The intensity of human capital formation

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 $\Omega_t^i \equiv$  characteristics affecting tech progress in country i:

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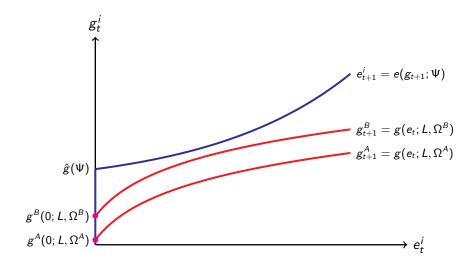
- Protection of intellectual property rights (policy)
- The stock of knowledge within a society
- The propensity of a country to trade (geography & policy)
  - Technological diffusion
  - Specialization and technological progress via learning by doing
  - Innovative Culture & Institutions

- Cultural and religious composition of society
  - Attitude toward knowledge creation and diffusion (e.g., The Inquisition)

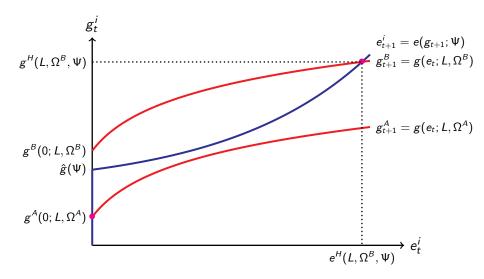
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  - Wider spectrum of traits are more likely to contain the ones complementary to the adoption or implementation of new technologies
- Abundance of natural resources
  - complementary for industrialization (e.g., Coal & Steam engine)



## Earlier Take-off in Country B



ullet For country-specific characteristics  $\Psi_t^i$ 

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- Ability of individuals to finance the cost of education and the forgone earnings
  - Extent of human capital formation

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- Cultural and religious composition of society
  - Attitude towards education affects the availability, quality and desirability of education

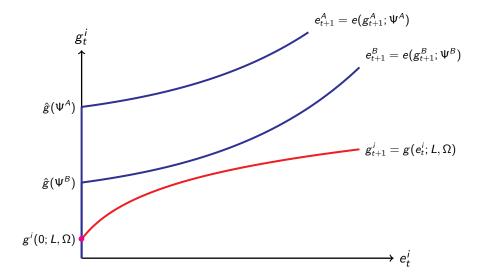
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  - Extent of human capital formation
- The availability, accessibility, and quality of public education (policy & interest groups)
  - Extent of human capital formation
- Cultural and religious composition of society
  - Attitude towards education affects the availability, quality and desirability of education
- The stock of knowledge in society
  - Productivity of human capital formation

- The propensity of a country to trade
  - Skill-intensity in production and its effect on the demand for human capital

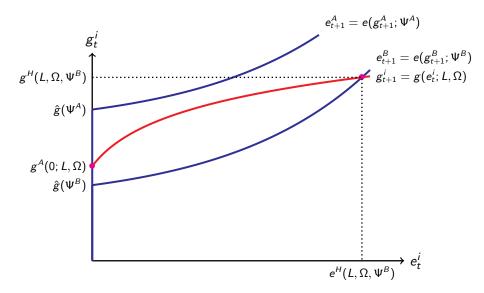
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- Social status associated with education



#### Earlier Take-off in Country B



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  - Human capital formation, triggered a demographic transition, enabling economies to convert a larger share of the fruits of factor accumulation and technological progress into growth of income per capita

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  - The transition from stagnation to growth was an inevitable by-product of the process of development
  - The inherent Malthusian interaction between technology and population, accelerated the pace of technological progress, and eventually brought an industrial demand for human capital
  - Human capital formation, triggered a demographic transition, enabling economies to convert a larger share of the fruits of factor accumulation and technological progress into growth of income per capita
  - Variations in the timing of the take-off contributed significantly to the divergence in income per capita in the past two centuries

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